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G-equivariant, bivariant algebraic K-theory

Let G be a group, \mathcal{F} a family of subgroups of G , \mathcal{C} a \mathbb{Z} -linear category equipped with a linear G -action, $\mathcal{C} \rtimes G$ the crossed product, and E a functor from \mathbb{Z} -linear categories to spectra. The G -equivariant E -homology with coefficients in \mathcal{C} associates a spectrum $H^G(X, E(\mathcal{C}))$ to every G -space X , in such a way that there is a weak equivalence $E(\mathcal{C} \rtimes H) \xrightarrow{\sim} H^G(G/H, E(\mathcal{C}))$. The *isomorphism conjecture* for the triple (G, \mathcal{F}, E) with coefficients in \mathcal{C} says that if $\mathcal{E}_{\mathcal{F}}G$ is a classifying space for G with respect to \mathcal{F} , then the map $\mathcal{E}_{\mathcal{F}}G \rightarrow G/G = pt$ induces a weak equivalence

$$H^G(\mathcal{E}_{\mathcal{F}}G, E(\mathcal{C})) \xrightarrow{\sim} E(\mathcal{C} \rtimes G)$$

When \mathcal{C} is a C^* -algebra, $\mathcal{F} = \mathit{Fin}$ is the family of finite subgroups $E = K^{\text{top}}$ and \rtimes is the reduced C^* -crossed product, this is the Baum-Connes conjecture with coefficients \mathcal{C} , and the groups in the left hand side

$$H_*^G(\mathcal{E}_{\mathit{Fin}}G, K^{\text{top}}(\mathcal{C})) = KK_*^G(\mathcal{E}_{\mathit{Fin}}G, \mathcal{C})$$

are the Kasparov equivariant bivariant K -theory groups. In the talk I will report about current progress on an old project that aims to describe the left hand side of the isomorphism conjecture for Weibel's homotopy algebraic K -theory in terms of Ellis' G -equivariant bivariant algebraic K -theory.